# **MODELICA LANGUAGE** EQUATION BASED COMPONENTS

Lecture 3.1





# OVERVIEW

- Modelica class container
- Accessing the source code
- Modelica at a glance
- Variables and types
- Arrays and matrices
- Equation and algorithm
- Operators and statements
- Connectors and connect()
- Balancing concept and partial
- Inheritance v/s Instantiation



# **MODELICA CLASS CONTAINER**

# CLASSES – INFORMATION CONTENT

• Modelica classes are containers with information, defined by the Modelica Language Specification





# DIFFERENT KEYWORDS FOR CLASSES

- **class**: any object is a class used only when unspecific, e.g. documentation classes
- package: container for more classes used to structure a set of models or a set of properties (e.g. fluid properties). Can only contain classes and constants
- **connector**: defines interfaces of models
- **model**: main class for physical behavior representation, using equations
- **block**: class for block diagrams require input/output connectors
- **function**: to implement algorithm that relate output to input variables
- **record**: container for variables of any variability
- **type**: "refined class" so that its instance would be more specific e.g. enumeration.
- (operator: mostly used for building blocks of your model e.g. Complex() )



# WHAT A MODEL SHOULD CONTAIN



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# ACCESSING THE SOURCE CODE

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# SOURCE CODE EDITOR

- Modelon Impact provides a code editor to edit the Modelica source code
- Accessed through toolbar:



# CODE EDITOR

- Basic functionality •
- Includes syntax check
- Syntax needs to be ok to be able to save changes.

**P**-

```
Navigate class history
                                        Find
                                                                               Change editor theme
                                                 Replace
               Undo/Redo
                                                                                       CTRL+Click to navigate to class
                                                      Jump to line
                                                                                       (follow link)
                                                                             ۵ĵ۵
                                         Q
                                                     GΞ
                                                             Impact Light
Code
                 5
    2 model Resistor "Ideal linear electrical resistor"
        parameter .Modelica.Units.SI.Resistance R(start=1)
          "Resistance at temperature T ref";
    Δ
        parameter .Modelica.Units.SI.Temperature T ref=300.15 "Reference #emperature";
    5
        parameter .Modelica.Units.SI.LinearTemperatureCoefficient alpha=0
    6
          "Temperature coefficient of resistance (R actual = R*(1 + alpha*(T heatPort - T ref))";
    7
    8
        extends Modelica.Electrical.Analog.Interfaces.OnePort;
    9
        extends .Modelica.Electrical.Analog.Interfaces.ConditionalHeatPort(T=T ref);
   10
        .Modelica.Units.SI.Resistance R_actual
   11
          "Actual resistance = R*(1 + alpha*(T_heatPort - T ref))";
   12
   13
   14 equation
        assert((1 + alpha*(T_heatPort - T_ref)) >= .Modelica.Constants.eps,
   15
          "Temperature outside scope of model!");
   16
        R actual = R*(1 + alpha*(T heatPort - T ref));
   17
   18
        v = R actual*i;
        LossPower = v*i;
   19
        annotation (••••);
  20
   58 end Resistor;
   59
```



# LOCAL BALANCE CHECK

 Checks semantics, and local balance of variables and equations





# MODELICA AT A GLANCE

# MODELICA AT A GLANCE

Modelica

- Object-oriented  $\rightarrow$  signalVoltage.V
- Acausal  $\rightarrow$  U = R\*I (no need to provide variants I := U/R or R = U/I)
- Type-based → Real vs Integer vs Boolean vs Modelica.Slunits.Voltage
- More complex structures such as partial, replaceable model etc.

The model class is divided into two main sections

- before the *equation* keyword contains all component, parameters, inputs, outputs and variable declarations
- 2. after the *equation* keyword contains all equations and connects





# VARIABLES AND TYPES

- Available default variable types:
  - Real floating point variable, e.g. 1.0, -2.3e-5
  - Integer integer variable, e.g. 1, 4, -333
  - Boolean boolean variable, e.g. false, true
  - String string, e.g. "from file:"
- Attributes of Real variables:
  - quantity type of physical quantity
  - unit unit used in equations
  - displayUnit used in dialogs and postprocessing
  - min minimal value of quantity
  - max maximum value of quantity
  - nominal used for scaling in numerical routines



# WHY FOCUS ON UNITS?

• Mars Climate Orbiter Failure Board Release Report, Nov. 10, 1999:

"The 'root cause' of the loss of the spacecraft was the failed **translation** of **English units** into **metric units** in a segment of ground-based, navigation-related mission software, as NASA has previously announced," said Arthur Stephenson, chairman of the Mars Climate Orbiter Mission Failure Investigation Board.

#### Ref:

https://www.jpl.nasa.gov/missions/mars-climate-orbiter





• Modelica.Slunits contains all 450 ISO-standard units as predefined variable types.



• Declarations using SI units package:

```
model HeatCapacitor "Lumped thermal element storing heat"
    parameter Modelica.SIunits.HeatCapacity C
        "Heat capacity of element (= cp*m)";
    Modelica.SIunits.Temperature T(start=293.15, displayUnit="degC")
        "Temperature of element";
    Modelica.SIunits.TemperatureSlope der_T(start=0)
        "Time derivative of temperature (= der(T))";
    Interfaces.HeatPort_a port annotation (...);
    equation
    T = port.T;
    der_T = der(T);
    C*der(T) = port.Q_flow;
    annotation (...);
end HeatCapacitor;
```

• In order to avoid repeating the package name at each declaration, create a package shortcut:

```
model HeatCapacitor "Lumped thermal element storing heat"
    import SI = .Modelica.SIunits;
    parameter SI.HeatCapacity C "Heat capacity of element (= cp*m)";
    SI.Temperature T(start = 293.15,displayUnit = "degC") "Temperature of element";
    SI.TemperatureSlope der_T(start = 0) "Time derivative of temperature (= der(T))";
    .Modelica.Thermal.HeatTransfer.Interfaces.HeatPort_a port annotation(...);
equation
    T=port.T;
    der_T=der(T);
    C * der(T)=port.Q_flow;
    annotation(...);
end HeatCapacitor;
```



- Time variability is set with a variable prefix:
  - no prefix variable can change with time
  - parameter parameter constant with time, may be modified
  - **constant** constant constant with time, may not be modified

```
1 partial model HeatCapacitance "Shperical heat capacitance"
2 import SI = Modelica.Slunits;
3 parameter SI.Diameter d "Sphere diameter";
4 parameter SI.Density rho "Density";
5 parameter SI.SpecificHeatCapacity c "heat capacity";
6 final parameter SI.Mass m = pi/6*d^3*rho "mass";
7 constant SI.DimensionlessRatio pi=Modelica.Constants.pi "pi";
8 SI.Temperature T "temperature";
9 SI.HeatFlowRate q_flow(nominal=10000) "heat flow rate";
10 equation
11
12 annotation(....);
13 end HeatCapacitance;
```

- In a component of the model above only **d**, **rho** and **c** can be modified at the container level
- A default equation may be added for the parameter declarations

 The model shall describe a spherical capacitance. Its mass is computed from diameter d and density rho:

```
1 partial model HeatCapacitance "Shperical heat capacitance"
2 import SI = Modelica.SIunits;
3 parameter SI.Diameter d "Sphere diameter";
4 parameter SI.Density rho "Density";
5 parameter SI.SpecificHeatCapacity c "heat capacity";
6 final parameter SI.Mass m = pi/6*d^3*rho "mass";
7 constant SI.DimensionlessRatio pi=Modelica.Constants.pi "pi";
8 SI.Temperature T "temperature";
9 SI.HeatFlowRate q_flow(nominal=10000) "heat flow rate";
10 equation
11
12 annotation(...);
13 end HeatCapacitance;
```

- In order to prevent it from appearing in the parameter dialog of the corresponding component and being modified with an inconsistent value, m received the final prefix
- The variables used in the default equation must not have a higher variability than the declared variable itself, i.e., for parameters only parameters and constants are allowed



**Declaration of multidimensional arrays:** 

parameter Real v1[3] = {1,2,3};

{} is array constructor of arrays with arbitrary dimension.

parameter Real v2[3,1] = [1;2;3];  $\begin{bmatrix} 1\\2\\3 \end{bmatrix}$ 

[] generates matrices, and acts as concatenation operator.

parameter Real m1[2,3] = {{11,12,13}, {21,22,23}};  $\begin{bmatrix} 11 & 12 & 13 \\ 21 & 22 & 23 \end{bmatrix}$ parameter Real m2[2,3] = [11, 12, 13; 21, 22, 23];  $\begin{bmatrix} 11 & 12 & 13 \\ 21 & 22 & 23 \end{bmatrix}$ parameter Real m3[3,3] = [m1; transpose([v])];

":" in the declaration section is used, when size of the array is undefined

parameter Real v[:]; // Size not defined yet

```
parameter Real A[:,:];
```

Access to matrix elements:

M2[2,3] // element [2,3] of Matrix M2

Vector constructor normally used to generate an indices-vector:

- 1:4 // generates {1,2,3,4}
- 1:2:7 // generates {1,3,5,7}

Extraction mechanism of sub-matrices as in Matlab:

M2[2:4,3] // generates {M2[2,3], M2[3,3], M2[4,3]}



• Operations according to standard mathematics. Compared to e.g. Matlab, it is worth noticing that Modelica handles physical vectors, i.e.:

vector\*vector = scalar [for ex:{1,2,3}\*{4,5,6} = 32]
matrix\*vector = vector [for ex:[1,2,3;4,5,6]\*{1,2,3}={14, 32}]
vector\*matrix = vector [for ex:{1,2,3}\*[4;5;6]={32}]
matrix\*matrix = matrix [for ex:[1;2]\*[3,4]=[3, 4;6, 8]]

• Creating an array of a general expression with an array constructor:

```
v = {i^2 for i in {1,3,7,6}}; // generates {1,9,49,36}
```

- M = V.\*d; // dot-notation for element-wise operation
- M = {V[i]\*d[i] for i in 1:n}; // equivalent

```
A = outerproduct(b,c);
```

```
A = {b[i]*c[j] for j in 1:m, i in 1:n}; // equivalent
```

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# **EQUATIONS AND ALGORITHMS**

# EQUATIONS

- Equations are added in the equation section after the **equation** keyword
- time is a global built-in variable
- Differential equations are expressed with the der-operator. It denotes the time derivative of the expression:

```
SI.Temperature T "temperature";
SI.HeatFlowRate q_flow(nominal=10000) "heat flow rate";
equation
  der(T)*m*c = Q_flow;
```

 Order of equations and which of the variables are located on the left or right-hand side of the equality sign is irrelevant



# INCLUDING CONNECTORS

- The example model has two time-varying variables and just one equation. The heat flow rate is determined outside the capacitance and shall cross its boundary through a connector.
  - 1. On the modeling canvas, drag in a component of the connector class Modelica.Thermal.HeatTransfer.Interfaces.HeatPort a
  - 2. Create a relationship between connector variables and variables declared in the model

```
.Modelica.SIunits.Temperature T "temperature";
.Modelica.SIunits.HeatFlowRate q_flow(nominal = 10000) "heat flow rate";
.Modelica.Thermal.HeatTransfer.Interfaces.HeatPort_a port_a annotation(....);
equation
    der(T)*m*c = Q_flow;
    Q_flow = port_a.Q_flow;
    T = port_a.T;
```



# INITIALIZATION

- Integrated variables require a start value, to solve the initial time problem
- They are set in an **initial equation** section, which is only evaluated at **time** = 0

```
parameter Modelica.SIunits.Temperature T_start "initial temperature";
.Modelica.SIunits.Temperature T "temperature";
.Modelica.SIunits.HeatFlowRate q_flow(nominal = 10000) "heat flow rate";
.Modelica.Thermal.HeatTransfer.Interfaces.HeatPort_a port_a annotation(...);
equation
    der(T) * m * c=Q_flow;
    Q_flow=port_a.Q_flow;
    T=port_a.T;
initial equation
    T = T_start;
```

 It is common practice to introduce a start value parameter, here T\_start, which can be propagated through the component levels.



# INITIALIZATION, FIXED =TRUE/FALSE

• Alternative way to set start values:

set start-attribute in variable declaration

parameter .Modelica.SIunits.Temperature T\_start "initial temperature"; .Modelica.SIunits.Temperature T(start=T\_start, fixed=true) "temperature";

- Difference to initial equations:
  - the start-attribute value is only used as an initial value of variable T if this is a state variable, i.e. an integration variable in the numerical solver. By setting fixed=true it generates an initial equation.
  - if the start-attribute is set for an **algebraic variable**, this value may be used by the solver as a **guess value** for iteration variables in non-linear initial equations.
  - The number of equations in the initial equation section is restricted to the degrees of freedom of the simulation experiment, i.e. the number of state variables. (Same holds for the number of fixed=true)



# ALGORITHMS

- The standard way in Modelica is to write equations, but also algorithms can be used, instead of 'equation' use 'algorithm' and instead of '=' use ':='.
- Algorithms are treated as a sequence of assignments.
- It is possible to use both an algorithm section and equation sections in the same model, but maximum one algorithm section.
- A value that is not assigned in an algorithm is assumed to be zero. There is no error message!



# IF STATEMENTS / FOR LOOPS

• The syntax is (same for both algorithm and equation)

```
if condition1 then
    expression1;
elseif condition2 then
    expression2;
else;
    expression3;
end if;
```

for ident in range loop
 expression;
end for;

NOTE: in equation sections, number of variables and equations must match, so no overwriting is possible.



# **OPERATORS AND STATEMENTS**

# DEVELOPING MODELS BY CODING

Equations are written in the equation section

- der()  $\rightarrow$  operator to indicate a time derivative of a variable
- connect() → operator to describe a connection between connectors connect() corresponds to a set of equations (discussed in part 2)
- if-, when-, while-statements etc. can be included



# CONNECTORS AND CONNECT()

# CONNECTORS

- To make the components interact with each other, we need clear interfaces: Connectors
- Key for the connector concept is the difference between potential and flow variables
- Each component must have a set of equations that uniquely define its behavior based on its interfaces and initial conditions.
- The components and the connectors need to be balanced, i.e. the number of unknowns and equations must match.
- In a Modelica connector, a variable with the **flow** prefix is a flow variable, and a variable without a prefix is a potential variable.



## POTENTIAL AND FLOW VARIABLES



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# POTENTIAL AND FLOW VARIABLES



# POTENTIAL AND FLOW VARIABLES

#### Heat transfer



# connector HeatPort Temperature T; flow HeatFlowRate Q\_flow; end HeatPort;

thermalC1.heatPort\_b.T = thermalC2.heatPort\_a.T
thermalC1.heatPort\_b.Q\_flow + thermalC2.heatPort\_a.Q\_flow = 0

#### **Rotational**

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connector Flange
Angle phi;
flow Torque tau;
end Flange;

inertia1.flange\_a.phi = inertia2.flange\_b.phi
inertia2.flange\_a.tau + inertia2.flange\_b.tau = 0

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#### **BALANCING CONCEPT AND PARTIAL**

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- A balanced model provides a set of equations so that either the flow or the potential variable can be solved for.
- In Modelica, all models should be "locally balanced"
- A model build from locally balanced sub-models is also balanced.
- This in turn requires that each connector has the same amount of flow and potential variables.



• In the examples below, each component has two connectors, each with one flow/potential variable. So two equations are needed, one for each flow/potential variable.

```
connector Pin
Modelica.SIunits.Voltage v;
flow Modelica.SIunits.Current i;
annotation(•••);
end Pin;
```

```
model Resistor
    parameter Real R;
equation
    p.i + n.i = 0;
    p.v - n.v = R*n.i;
end Resistor;
```

```
connector Flange
.Modelica.SIunits.Position s;
flow .Modelica.SIunits.Force f;
annotation(••••);
end Flange;
```

```
model Spring
   parameter Real c;
equation
   flange_a.f + flange_b.f = 0;
   flange_b.f = c*(flange_b.s-flange_a.s);
end Spring;
```



- How are the number of equations and unknown calculated?
- Model Resistor is balanced:

```
connector Pin
                                           Unknowns:
    Modelica.SIunits.Voltage v;
                                            p.i, p.v, n.i, n.v
    flow Modelica.SIunits.Current i;
    annotation(....);
                                           Equations:
end Pin;
                                            p.i + n.i = 0;
                                            p.v - n.v = R*n.i;
model Resistor
   Electrical.Pin p;
                                           + 2 eqn for flow-variables
   Electrical.Pin n;
                                               p.i and n.i,
   parameter Real R;
equation
                                           when you check for local
   p.i + n.i = 0;
                                           balance
   p.v - n.v = R^*n.i;
end Resistor;
```



• Not all models have a relation between flow and potential, e.g. an electrical ground or a mechanical fixed:

model Fixed
••
equation
<pre>flange_a.s = 0;</pre>
end Fixed;

• As a result, these components cannot be connected to each other.



• The same holds for a model that directly supplies flow information, e.g. different types of sources.



# INHERITANCE V/S INSTANTIATION

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# **OBJECT-ORIENTATION**

#### • Extends



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# DEVELOPING MODELS BY CODING

Developing model using Modelica code

- Should be only when necessary (or for fun)
- Should reuse existing base classes as much as possible
- Requires much maintenance work and testing

#### Extension v/s Instantiation

- <u>extends</u> Modelica.Electrical.Analog.Interfaces.TwoPin
  - Model inherit all content from the extended classes (interfaces, equations, icon etc.)
  - All code from TwoPin will be inlined in the model
- Modelica.Electrical.Analog.Sources.SignalVoltage <a href="mailto:signalVoltage">signalVoltage</a>
  - Creates an instance of SignalVoltage called signalVoltage
  - Accessing variables of the instance through dot notation (e.g. signalVoltage.v)





# **OBJECT-ORIENTATION**

When to do what?

- Extend:
  - Interfaces, templates, icons  $\rightarrow$  common parts, partial
  - Physical effects  $\rightarrow$  abstraction of a phenomena
  - Flat model and results
- Instantiate:
  - Models, Records, etc.  $\rightarrow$  container / entity
  - "Physical components"  $\rightarrow$  model composition representing user expectations
  - Structured model and results



# WORKSHOP 3.1

In this workshop you will:

• Create a simple cake model

